Name_

у

А

40.0°

5.0

B

х

4.0

Feb. 3, 2012

Quiz #1 — Spring 2012 Phys 2110 – Sec 4

1. Convert $30.2 \frac{\text{cm}}{\text{s}}$ to units of $\frac{\text{km}}{\text{h}}$.

$$30.2 \, \frac{\mathrm{cm}}{\mathrm{s}} = (30.2 \, \frac{\mathrm{cm}}{\mathrm{s}}) \left(\frac{3600 \, \mathrm{s}}{1 \, \mathrm{h}}\right) \left(\frac{1 \, \mathrm{m}}{100 \, \mathrm{cm}}\right) \left(\frac{1 \, \mathrm{km}}{1000 \, \mathrm{m}}\right) = 1.09 \, \frac{\mathrm{km}}{\mathrm{h}}$$

2. Vector A has magnitude 5.00 and points at angle $\theta = 40.0^{\circ}$ above the x axis. Vector B has magnitude 4.00 and a direction such that $\mathbf{A} + \mathbf{B}$ points in the x direction, as shown.

a) Find B_y .

The $y-{\rm components}$ of the two vectors must add up to zero: $A_y+B_y=0.$ So, since

$$A_y = A \sin \theta_A = (5.00) \sin 40^\circ = 3.21$$
 then $B_y = -A_y = -3.21$

b) If **B** points at an angle between 0.00° and -90.0° (as the picture indicates), find the direction of **B**.

If ϕ is the direction of **B** then

$$B_y = B\sin\phi \implies \sin\phi = \frac{B_y}{B} = \frac{-3.21}{4.0} = -0.803$$

This gives

$$\phi = \sin^{-1}(-0.803) = -53.5^{\circ}$$

which is in the correct quadrant. So $\phi = -53.5^{\circ}$,

3. A projectile is fired upward from floor level inside a room with a ceiling of height 15.0 m. The launch speed of the projectile is $16.0 \frac{\text{m}}{\text{s}}$.

a) Will the projectile hit the ceiling? Explain how you know.

If there were no ceiling then we would solve for the maximum height by solving for the value of y where the velocity is zero. Use:

$$v^{2} = v_{0}^{2} + 2ay \qquad \Longrightarrow \qquad y = \frac{v^{2} - v_{0}^{2}}{2a} = \frac{0 - (16.0 \, \frac{\text{m}}{\text{s}})^{2}}{(-9.80 \, \frac{\text{m}}{\text{s}^{2}})} = 13.1 \, \text{m}$$

The maximum height is less than the height of this room, so that with the ceiling the projectile never gets up to $15.0 \,\mathrm{m}$ to strike it. The projectile does not hit the ceiling.

 \mathbf{b}_{1} If it *does* hit, with what speed does it strike the ceiling and how long did it take to reach the ceiling?

 \mathbf{b}_{2} If it *doesn't* hit, what was the maximum height attained by the projectile and how long did it take to get to maximum height?

The answer was already found in (a), namely 13.1 m. Next find the time in the flight when the velocity was zero:

$$v = v_0 + at = 0 \qquad \Longrightarrow \qquad t = \frac{v - v_0}{a} = \frac{0 - 16.0 \,\frac{\mathrm{m}}{\mathrm{s}}}{(-9.80 \,\frac{\mathrm{m}}{\mathrm{s}^2})} = 1.63 \,\mathrm{s}$$

so it takes 1.63s to get to maximum height.

Just answer one of the (b)'s. Don't answer both.

You must show all your work and include the right units with your answers!

$$A_{x} = A \cos \theta \qquad A_{y} = A \sin \theta \qquad A = \sqrt{A_{x}^{2} + A_{y}^{2}} \qquad \tan \theta = \frac{A_{y}}{A_{x}}$$
$$v = v_{0} + at \qquad x = x_{0} + v_{0}t + \frac{1}{2}at^{2} \qquad v^{2} = v_{0}^{2} + 2a(x - x_{0}) \qquad x - x_{0} = \frac{1}{2}(v_{0} + v)t$$
$$g = 9.80 \frac{m}{s^{2}} \qquad 1 h = 60 \min \qquad 1 \text{ km} = 10^{3} \text{ m} \qquad \text{Ignore air resistance.}$$

